

t-test

Introduction :- In the experiments of different schools of S.S.T., especially when the effects of two factors are considered, it becomes essential to compare the means of two samples and to draw a meaningful conclusion before interpreting the results.

While comparing two samples on a quantitative basis, the variables are usually arranged in a table to facilitate comparison of means of two samples. It seems essential because visual expressions of the difference between the means of two samples, often does not prove that there is, in fact, a significant difference between the means of two samples. At that time it becomes difficult to draw a conclusion about which of the two means is significantly greater, than the other. Even if one is greater, it is essential to decide to what extent it is greater than the other. The degree or level of significance of this difference is to be quantified so that a meaningful conclusion and idea can be developed.

To attach a statistical significance of such a difference (or no difference) a statistical test is applied known as the t-test. It was introduced by W.S. Gossett (1908) under nom de plume of 'student'. The real name of Gossett was Student and therefore t-test is also known as student t-test. Its multifold explanation was developed by Fischer. It is based on the principle of null hypothesis.

Definitions : (i) According to Gossett: t is a critical ratio in which more exact estimate

of standard deviation of difference between two means is used.

- (2) t -test is the statistic through which the significance of difference between two groups (either correlated or uncorrelated) is tested.
- (3) t -test is a ratio of difference between two means and standard error of difference between two means i.e.,

$$t = \frac{\text{Difference between two means}}{\text{Standard error of difference between two means}}$$

Characteristics: - (1) The difference between the means of two variables may be due to variability of data in samples and thus the difference between the means has no significance.

- (2) It tests the significant difference of two means, when the groups are small.
- (3) The sampling distribution of t is normal when n is larger.
- (4) Its value changes with the degree of freedom.
- (5) It gives accurate estimate when n is less than 30.
- (6) It utilizes both the means and standard deviations of two samples.
- (7) It gives interval estimation of small samples.

Uses: - To find out bilateral limits: If we choose a value of probability of occurrence of true mean to lie in a range on either side of the sample mean and then we can find out corresponding t -values with the degree of freedom. Now, we can have the limits with t -value, sample mean and